# Artificial Intelligence CE-417, Group 1 Computer Eng. Department Sharif University of Technology

Fall 2023

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Courtesy: Most slides are adopted from CSE-573 (Washington U.), original slides for the textbook, and CS-188 (UC. Berkeley).



# **Reinforcement Learning**

Warm

Overheated

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#### Still assume a markov decision process (MDP):

- A set of states  $s \in S$
- A set of actions (per state) A
- A model T(s,a,s')
- A reward function R(s,a,s')
- Still looking for a policy  $\pi(s)$



- i.e. We don't know which states are good or what the actions do
- Must actually try actions and states out to learn

# **Reinforcement Learning**

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- New twist: don't know T or R
  - i.e. We don't know which states are good or what the actions do
  - Must actually try actions and states out to learn



# Example: Learning to Walk



Initial



#### A Learning Trial



#### After Learning [1K Trials]

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[Kohl and Stone, ICRA 2004]



# Example: Learning to Talk

#### ChatGPT: Optimizing Language Models for Dialogue

We've trained a model called ChatGPT which interacts in a conversational way. The dialogue format makes it possible for ChatGPT to answer followup questions, admit its mistakes, challenge incorrect premises, and reject inappropriate requests. ChatGPT is a sibling model to <u>InstructGPT</u>, which is trained to follow an instruction in a prompt and provide a detailed response.

November 30, 2022 13 minute read







# Passive Reinforcement Learning

#### Simplified task: policy evaluation

- Input: a fixed policy  $\pi(s)$
- You don't know the transitions T(s,a,s')
- You don't know the rewards R(s,a,s')
- Goal: learn the state values



- In this case:
  - Learner is "along for the ride"
  - No choice about what actions to take
  - Just execute the policy and learn from experience
  - This is NOT offline planning! You actually take actions in the world.



# **Model-Based Learning**

- Model-based idea:
  - Learn an approximate model based on experiences
  - Solve for values as if the learned model were correct
- Step 1: learn empirical MDP model

  - Count outcomes s' for each s, a Normalize to give an estimate of  $\widehat{T}(s, a, s')$
  - Discover each  $\widehat{R}(s,a,s')$  when we experience (s, a, s')
- Step 2: solve the learned MDP
  - For example, use value iteration, as before









# Analogy: Expected Age

Goal: Compute expected age of cs188 students

Knowr	ר P(A)	
$E[A] = \sum_{a} P(a) \cdot a$	$= 0.35 \times 20 + \dots$	
a		

Without P(A), instead collect samples  $[a_1, a_2, ..., a_N]$ 





# **Direct Evaluation**

• Goal: compute values for each state under  $\pi$ 

- Idea: average together observed sample values
  - Act according to  $\pi$
  - Every time you visit a state, write down what the sum of discounted rewards turned out to be from that state until the end of sample<sub>i</sub>(s) =  $R(s) + \gamma R(s') + \gamma^2 R(s'') + ...$
  - Average those sample  $V(s) \leftarrow \frac{1}{N} \sum_{i} sample_{i}(s)$
- This is called direct evaluation





V(s) is sum of discounted rewards from s until the end, averaged over all encounters of s

# **Problems with Direct Evaluation**

#### What's good about direct evaluation?

- It's easy to understand
- It doesn't require any knowledge of T, R
- It eventually computes the correct average values, using just sample transitions
- What bad about it?
  - It wastes information about state connections
  - Each state must be learned separately so, it takes a long time to learn
  - Need to have all episodes ahead of time (cannot "stream" in transitions)

#### **Output Values**



If B and E both go to C under this policy, how can their values be different?

# Why Not Use Policy Evaluation?

**π(s)** 

s, π(s)

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\_s, π(s),s'

Simplified Bellman updates calculate V for a fixed policy:

• Each round, replace V with a one-step-look-ahead layer over V

$$V_0^{\pi}(s) = 0$$
  
$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

- This approach fully exploited the connections between the states
- Unfortunately, we need T and R to do it!
- Key question: how can we do this update to V without knowing T and R?
  - In other words, how to we take a weighted average without knowing the weights?

# Sample-Based Policy Evaluation?

• We want to improve our estimate of V by computing these averages:  $V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$ 

• Idea: take samples of outcomes s' (by doing the action!) and average

$$sample_{1} = R(s, \pi(s), s'_{1}) + \gamma V_{k}^{\pi}(s'_{1})$$

$$sample_{2} = R(s, \pi(s), s'_{2}) + \gamma V_{k}^{\pi}(s'_{2})$$
...
$$sample_{n} = R(s, \pi(s), s'_{n}) + \gamma V_{k}^{\pi}(s'_{n})$$

$$V_{k+1}^{\pi}(s) \leftarrow \frac{1}{n} \sum_{i} sample_{i}$$



# **Temporal Difference Learning**

#### Big idea: learn from every experience!

- Update V(s) each time we experience a transition (s, a, s', r)
- Likely outcomes s' will contribute updates more often
- Temporal difference learning of values
  - Policy still fixed, still doing evaluation!
  - Move values toward value of whatever successor occurs: running average

Sample of V(s):  $sample = R(s, \pi(s), s') + \gamma V^{\pi}(s')$ Update to V(s):  $V^{\pi}(s) \leftarrow (1 - \alpha)V^{\pi}(s) + (\alpha)sample$ Same update:  $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha(sample - V^{\pi}(s))$ 



# **Exponential Moving Average**

#### Exponential moving average

• The running interpolation update:

$$\bar{x}_n = (1 - \alpha) \cdot \bar{x}_{n-1} + \alpha \cdot x_n$$

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• Makes recent samples more important:

$$\bar{x}_n = \frac{x_n + (1 - \alpha) \cdot x_{n-1} + (1 - \alpha)^2 \cdot x_{n-2} + \dots}{1 + (1 - \alpha) + (1 - \alpha)^2 + \dots}$$

- Forgets about the past (distant past values were wrong anyway)
- Decreasing learning rate (alpha) can give converging averages



# TD Learning Happen in the Brain!

 Neurons transmit Dopamine to encode reward or value prediction error

 $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha (\text{sample} - V^{\pi}(s))$ 

• Example of Neuroscience & Al informing each other



# Problems with TD Value Learning

- TD value leaning is a model-free way to do policy evaluation, mimicking bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

 $\pi(s) = \arg\max_{a} Q(s, a)$ 

$$Q(s,a) = \sum_{s'} T(s,a,s') \left[ R(s,a,s') + \gamma V(s') \right]$$

- Idea: learn Q-values, not values
- Makes action selection model-free too!



# **Detour: Q-Value Iteration**

Value iteration: find successive (depth-limited) values

- Start with V<sub>0</sub>(s) = 0, which we know is right
- Given V<sub>k</sub>, calculate the depth k+1 values for all states:

$$V_{k+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[ R(s, a, s') + \gamma V_k(s') \right]$$

- But Q-values are more useful, so compute them instead
  - Start with Q<sub>0</sub>(s,a) = 0, which we know is right
  - Given Q<sub>k</sub>, calculate the depth k+1 Q-values for all Q-states:

$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[ R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

# Q-Learning

Q-learning: sample-based q-value iteration

$$Q_{k+1}(s,a) \leftarrow \sum_{s'} T(s,a,s') \left[ R(s,a,s') + \gamma \max_{a'} Q_k(s',a') \right]$$

- Learn Q(s,a) values as you go
  - Receive a sample (s,a,s',r)
  - Consider your old estimate: Q(s, a)
  - Consider your new sample estimate:

 $sample = R(s, a, s') + \gamma \max_{a'} Q(s', a')$ 

• Incorporate the new estimate into a running average:

 $Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha) [sample]$ 



# Wideo of Demo Q-Learning -- Gridworld



# Video of Demo Q-Learning -- Crawler



# **Q-Learning Properties**

 Amazing result: Q-learning converges to optimal policy -- even if you're acting sub-optimally!

- This is called off-policy learning
- Caveats:
  - You have to explore enough
  - You have to eventually make the learning rate small enough
  - ... but not decrease it too quickly
  - Basically, in the limit, it doesn't matter how you select actions (!)



# Active Reinforcement Learning 32

# Active Reinforcement Learning

• Full reinforcement learning: optimal policies (like value iteration)

- You don't know the transitions T(s,a,s')
- You don't know the rewards R(s,a,s')
- You choose the actions now
- Goal: learn the optimal policy / values

- In this case:
  - Learner makes choices!
  - Fundamental tradeoff: exploration vs. exploitation
  - This is NOT offline planning! You actually take actions in the world and find out what happens...



# Video of Demo Q-learning – Manual Exploration – Bridge Grid



# How to Explore?

#### Several schemes for forcing exploration

- Simplest: random actions (E-greedy)
  - Every time step, flip a coin
  - With (small) probability  $\varepsilon$ , act randomly
  - With (large) probability  $1-\varepsilon$ , act on current policy
- Problems with random actions?
  - You do eventually explore the space, but keep thrashing around once learning is done
  - One solution: lower  $\epsilon$  over time
  - Another solution: exploration functions



# Video of Demo Q-learning – Epsilon-Greedy – Crawler

# **Exploration Functions**

#### • When to explore?

- Random actions: explore a fixed amount
- Better idea: explore areas whose badness is not (yet) established, eventually stop exploring
- Exploration function
  - Takes a value estimate u and a visit count n, and returns an optimistic utility, e.g. f(u,n) = u + k/n



[Demo: exploration – Q-learning – crawler – exploration function (L11D4)]

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Regular Q-update:  $Q(s,a) \leftarrow_{\alpha} R(s,a,s') + \gamma \max_{a'} Q(s',a')$ 

• Note: this propagates the "bonus" back to states that lead to unknown states as well! Modified Q-update:  $Q(s,a) \leftarrow_{\alpha} R(s,a,s') + \gamma \max_{s} f(Q(s',a'), N(s',a'))$ 

 $x \leftarrow_a v$  is shorthand for  $x \leftarrow (1 - \alpha)x + \alpha v$ 

Video of Demo Q-learning – Exploration Function – Crawler

How Can we Evaluate Exploration Methods?

Regret

- Even if you learn the optimal policy, you still make mistakes along the way!
- Regret is a measure of your total mistake cost: the difference between your (expected) rewards, including youthful suboptimality, and optimal (expected) rewards
- Minimizing regret goes beyond learning to be optimal – it requires optimally learning to be optimal
- Example: random exploration and exploration functions both end up optimal, but random exploration has higher regret

# 2 Con

# Approximate Q-Learning



# **Generalizing Across States**

Basic Q-learning keeps a table of all Q-values

- In realistic situations, we cannot possibly learn about every single state!
  - Too many states to visit them all in training
  - Too many states to hold the q-tables in memory
- Instead, we want to generalize:
  - Learn about some small number of training states from experience
  - Generalize that experience to new, similar situations
  - This is a fundamental idea in machine learning, and we'll see it over and over again



[demo – RL pacman]

Let's say we discover through experience that this state is bad:

# **Example:** Pacman

In naïve Q-learning, we know nothing about this state:

#### Or even this one!







# Video of Demo Q-Learning Pacman — Tiny — Watch All 🔘

# Video of demo Q-learning Pacman — tiny — silent train 🔘

# Video of Demo Q-Learning Pacman – Tricky – Watch All



# Feature-Based Representations

- Solution: describe a state using a vector of features (properties)  $f_1, f_2, \ldots$ 
  - Features are functions from states to real numbers (often 0/1) that capture important properties of the state
  - Example features:
    - Distance to closest ghost
    - Distance to closest dot
    - Number of ghosts
    - 1 / (dist. to dot)<sup>2</sup>
    - Is Pacman in a tunnel? (0/1)
    - ..... Etc.
    - Is it the exact state on this slide?
  - Can also describe a q-state (s, a) with features (e.g. Action moves closer to food)



# **Linear Value Functions**

• Using a feature representation, we can write a Q function (or value function) for any state using a few weights:

$$V(s) = w_1 f_1(s) + w_2 f_2(s) + \ldots + w_n f_n(s)$$

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$$

- Advantage: our experience is summed up in a few powerful numbers  $W_1, W_2, ...$
- Disadvantage: states may share features but actually be very different in value!
  - Ex: these two states would have the same value if we don't include ghost positions as a feature:



# Approximate Q-Learning

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$$

• Q-learning with linear q-functions:

$$\begin{array}{l} \text{transition} &= (s, a, r, s') \\\\ \text{difference} &= \left[ r + \gamma \max_{a'} Q(s', a') \right] - Q(s, a) \\\\ Q(s, a) \leftarrow Q(s, a) + \alpha \left[ \text{difference} \right] \qquad \text{Exact Q's} \\\\ w_i \leftarrow w_i + \alpha \left[ \text{difference} \right] f_i(s, a) \qquad \text{Approximate Q's} \end{array}$$

- Intuitive interpretation:
  - Adjust weights of active features
  - e.g., If something unexpectedly bad happens, blame the features that were on: disprefer all states with that state's features
- Formal justification: online least squares, gradient descent



$$Q(s,a) = 4.0 f_{DOT}(s,a) - 1.0 f_{GST}(s,a)$$



$$Q(s, \text{NORTH}) = +1$$
  
$$r + \gamma \max_{a'} Q(s', a') = -500 + 0$$

difference = -501  $\longrightarrow$   $w_{DOT} \leftarrow 4.0 + \alpha [-501] 0.5$  $w_{GST} \leftarrow -1.0 + \alpha [-501] 1.0$ 

 $Q(s,a) = 3.0 f_{DOT}(s,a) - 3.0 f_{GST}(s,a)$ 

[Demo: approximate Qlearning pacman (L11D10)]

# Video of Demo Approximate Q-Learning -- Pacman





# Linear Approximation: Regression\*



Prediction:  

$$\hat{y} = w_0 + w_1 f_1(x)$$



Optimization: Least Squares\*

total error = 
$$\sum_{i} (y_i - \hat{y}_i)^2 = \sum_{i} \left( y_i - \sum_k w_k f_k(x_i) \right)^2$$



# Minimizing Error\*

Imagine we had only one point x, with features f(x), target value y, and weights w:

$$\operatorname{error}(w) = \frac{1}{2} \left( y - \sum_{k} w_{k} f_{k}(x) \right)^{2}$$
$$\frac{\partial \operatorname{error}(w)}{\partial w_{m}} = - \left( y - \sum_{k} w_{k} f_{k}(x) \right) f_{m}(x)$$
$$w_{m} \leftarrow w_{m} + \alpha \left( y - \sum_{k} w_{k} f_{k}(x) \right) f_{m}(x)$$



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Approximate q update explained:

$$w_m \leftarrow w_m + \alpha \left[ r + \gamma \max_a Q(s', a') - Q(s, a) \right] f_m(s, a)$$
  
"target" "prediction"

# Conclusion

- We're done with part I: search and planning!
- We've seen how AI methods can solve problems in:
  - Search
  - Constraint satisfaction problems
  - Games
  - Markov decision problems
  - Reinforcement learning





# **Policy Search**

- Problem: often the feature-based policies that work well (win games, maximize utilities) aren't the ones that approximate V / Q best
  - Q-learning's priority: get Q-values close (modeling)
  - Action selection priority: get ordering of Q-values right (prediction)
  - We'll see this distinction between modeling and prediction again later in the course
- Solution: learn policies  $\pi$  that maximize rewards, not the Q values that predict them



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 Policy search: start with an ok solution (e.g. Q-learning) then fine-tune by hill climbing on feature weights

# **Policy Search**

- Simplest policy search:
  - Start with an initial linear value function or Q-function
  - Nudge each feature weight up and down and see if your policy is better than before

- Problems:
  - How do we tell the policy got better?
  - Need to run many sample episodes!
  - If there are a lot of features, this can be impractical
- Better methods exploit lookahead structure, sample wisely, change multiple parameters...
  - Policy Gradient, Proximal Policy Optimization (PPO) are examples

# Case Studies of Reinforcement Learning!

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• Atari game playing

Robot Locomotion

• Language assistants

# Case Studies: Atari Game Playing



# Case Studies: Atari Game Playing

- MDP:
  - State: image of game screen
    - 256<sup>84\*84</sup> possible states
    - Processed with hand-designed feature vectors or neural networks
  - Action: combination of arrow keys + button (18)
  - Transition T: game code (don't have access)
  - **Reward R:** game score (don't have access)
- Very similar to our pacman MDP
- Use approximate Q learning with neural networks and ε-greedy exploration to solve





[Human-level control through deep reinforcement learning, Mnih et al, 2015]

# **Case Studies: Robot Locomotion**

• MDP:

- State: image of robot camera + N joint angles + accelerometer + ...
  - Angles are N-dimensional continuous vector!
  - Processed with hand-designed feature vectors or neural networks
- Action: N motor commands (continuous vector!)
  - Can't easily compute  $\max_{a} Q(s', a)$  when a is continuous
  - Use policy search methods or adapt Q learning to continuous actions
- Transition T: real world (don't have access)
- Reward R: hand-designed rewards
  - Stay upright, keep forward velocity, etc
- Learning in the real world may be slow and unsafe
  - Build a simulator and learn there first, then deploy in real world





# Case Studies: Language Assistants

# ChatGPT

#### Brainstorm edge cases

for a function with birthdate as input, horosco...

Show me a code snippet of a website's sticky header Come up with concepts for a retro-style arcade game

Recommend a dish to impress a date who's a picky eater

where is Tehran?



# Case Studies: Language Assistants

- Step 1: train large language model to mimic human-written text
  - Query: "Where is Tehran?"
  - Human-like completion: "This question always fascinated me!"
- Step 2: fine-tune model to generate **helpful** text
  - Query: "Where is Tehran?"
  - Helpful completion: "Tehran is the capital and largest city of Iran."
- Use Reinforcement Learning in Step 2

# Case Studies: Language Assistants

- MDP:
  - State: sequence of words seen so far (ex. "Where is Tehran?")
    - 100,000<sup>1000</sup> possible states
    - Huge, but can be processed with feature vectors or neural networks
  - Action: next word (ex. "It", "chair", "purple", ...) (so 100,000 actions)
    - Hard to compute max" Q(s', a) when max is over 100K actions!
  - Transition T: easy, just append action word to state words
    - s: "My name" a: "is" s': "My name is"
  - Reward R: ???
    - Humans rate model completions (ex. "Where is Tehran?")
      - "It is the capital and largest city of Iran": +1
      - "It is in google maps": -1
      - "Destroy all humans": -1
    - Learn a reward model  $\widehat{R}$  and use that (model-based RL)
- Commonly use policy search (Proximal Policy Optimization) but looking into Q Learning